Practice Assignment 5

In this fifth practice assignment, you will review topics from

7th edition: sections 6.6 , 8.6 , 10.1 and 10.2.

8th edition: sections 6.5 , 10.1 and 10.2 plus L'Hôpital's Rule.

Try all problems for practice.

If you have difficulties, ask for help in class or in the instructor's office; all answers are shown in another file.

$$\begin{array}{ll} (1) \lim_{x \to \infty} \frac{2x^3 + \sqrt{x}}{3 - 5x^3} & (2) \lim_{x \to 0} \frac{e^{-3x} + x^3 - 1}{1 - e^{5x}} & (3) \lim_{x \to 0} \frac{e^{x} - x^2 - 1}{\sin 2x} \\ (4) \lim_{x \to 0} \frac{e^{x} - x^3 - 1}{\sin \left(\frac{x}{2}\right)} & (5) \lim_{x \to \infty} \frac{4e^{3x} - x^2}{1 + x + 6e^{3x}} & (6) \lim_{x \to \infty} \frac{e^{2/x} - 3x^2}{4x^2 - e^{3/x}} \\ (7) \lim_{x \to 0} \frac{\cos 3x - 5x - 1}{\tan 2x} & (8) \lim_{x \to \pi} \frac{3 \sin x + 2 \tan 3x}{4 \tan 2x - x + \pi} & (9) \lim_{x \to 2} \frac{\cos \left(x - 2\right) + 2x - 5}{x - 4 + 2e^{x - 2}} \\ (10) \lim_{x \to \infty} \frac{\sqrt{x + 2} + 5\sqrt{x + 3}}{\sqrt{4x + 1}} & (11) \lim_{x \to 0} \frac{6x^3 - 5x}{e^x - 1} & (12) \lim_{x \to -2} \frac{3x^3 + 11x^2 + 8x - 4}{5x^3 + 21x^2 + 24x + 4} \\ (13) \lim_{x \to \infty} \frac{\left(3x - 4\right)^3}{9x^2 - 5x^3} & (14) \lim_{x \to \pi} \frac{\sin 3x + \pi - x}{2 - \sec \frac{2}{3} + \tan 2x} & (15) \lim_{x \to 2^+} \frac{2 - x - e^{x - 2}}{x^2 - 4} \\ (16) \int_4^{\infty} \frac{6}{(4 - 3x)^{1/3}} dx & (17) \int_{-\infty}^1 \frac{4x - 6}{(x^2 - 3x + 3)^3} dx & (18) \int_1^{\infty} \frac{6x}{9 + x^2} dx \\ (19) \int_{-\infty}^{-2} \frac{2x^3 + 1}{(x^4 + 2x)^3} dx & (20) \int_1^{\infty} 6x^2 e^{1 - x^3} dx & (21) \int_0^0 \frac{9x^2}{(x^3 + 1)^{5/3}} dx \\ (22) \int_0^{\infty} \frac{x^2 + 1}{(x^3 + 3x + 4)^{5/2}} dx & (23) \int_0^1 \frac{2x + 7}{\sqrt{x^2 + 7x - 8}} dx & (24) \int_0^1 \frac{e^{2x}}{1 - e^{2x}} dx \\ (25) \int_1^2 \frac{2x^2 + 1}{\sqrt{(2x^3 + 3x - 5)^3}} dx & (26) \int_3^7 \frac{e^{\sqrt{x - 3}}}{\sqrt{x - 3}} dx & (27) \int_0^{\pi/4} \cot 3x dx \\ (28) \int_0^{\pi/4} \sec 2x \tan 2x dx & (29) \int_0^{\pi/6} \frac{\sec^2 2x}{\sqrt{1 - \tan 2x}} dx & (30) \int_{-\infty}^{\pi/3} \frac{\sin 3x}{(1 + \cos 3x)^{2/3}} dx \\ (31) \lim_{x \to \infty} \frac{\sqrt{4x^2 + 3}}{9 - x} & (32) \lim_{x \to 0} \frac{4x + 1 - e^{2x}}{\sqrt{x^2 + x - 2}} dx \\ (34) \int_0^1 \frac{e^{\sqrt{x}}}{\sqrt{x} (e^{\sqrt{x}} + 1)^2} dx & (35) \int_1^2 \frac{2x + 1}{\sqrt{x^2 + x - 2}} dx \\ \end{cases}$$

Practice Assignment 5

(36) Determine whether the series $\sum_{n=1}^{\infty} \frac{1}{2} \left(\frac{5}{3}\right)^n$ converges or diverges. If the series converges, find its sum. (37) Determine whether the series $\sum_{n=0}^{\infty} \frac{5}{3} \left(\frac{1}{2}\right)^n$ converges or diverges. If the series converges, find its sum. (38) Determine whether the series $\sum_{n=0}^{\infty} 250 (1.2)^n$ converges or diverges. If the series converges, find its sum. (39) Determine whether the series $\sum_{n=1}^{\infty} 125 (0.2)^n$ converges or diverges. If the series converges, find its sum. (40) Determine whether the series $\sum_{n=1}^{\infty} \frac{4n^2 - n^3}{4 - n^2}$ converges or diverges. If the series converges, find its sum. (41) Determine whether the series $\sum_{n=1}^{\infty} \frac{(2+3n)(4+n^2)}{(2+n^2)(1+n)}$ converges or diverges. If the series converges, find its sum. (42) Determine whether the series $\sum_{n=1}^{\infty} 6\left(-\frac{2}{3}\right)^n$ converges or diverges. If the series converges, find its sum. (43) Determine whether the series $\sum_{n=1}^{\infty} 20 \left[\left(\frac{1}{4}\right)^n - \left(\frac{1}{5}\right)^n \right]$ converges or diverges. If the series converges, find its sum. (44) Determine whether the series $\sum_{n=1}^{\infty} \frac{1}{4} \left(\frac{5}{2}\right)^n$ converges or diverges. If the series converges, find its sum. (45) Determine whether the series $\sum_{n=1}^{\infty} \frac{\sqrt{9+n^2}}{n+1}$ converges or diverges. If the series converges, find its sum. (46) Determine whether the series $\sum_{n=1}^{\infty} \frac{n+n^3}{3+n}$ converges or diverges. If the series converges, find its sum. (47) Determine whether the series $\sum_{n=1}^{\infty} \frac{5}{3^n}$ converges or diverges. If the series converges, find its sum.

(48) Determine whether the series $\sum_{n=1}^{\infty} \frac{2^n}{5^{n+1}}$ converges or diverges. If the series converges, find its sum.

<u>Math 201-203-RE</u>

- (49) Determine whether the series $\sum_{n=1}^{\infty} \frac{3^{n+1}}{4^n}$ converges or diverges. If the series converges, find its sum.
- (50) Determine whether the series $\sum_{n=1}^{\infty} 4 \frac{2^{n+1}}{3^n}$ converges or diverges. If the series converges, find its sum.
- (51) Given a repeated decimal $4.\overline{13}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (52) Given a repeated decimal $6.\overline{04}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (53) Given a repeated decimal $3.\overline{09}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (54) Given a repeated decimal $2.\overline{02}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (55) Given a repeated decimal $5.\overline{011}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (56) Given a repeated decimal $1.\overline{06}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (57) Given a repeated decimal $2.\overline{03}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (58) Given a repeated decimal $8.\overline{01}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (59) Given a repeated decimal $2.\overline{22}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (60) Given a repeated decimal $5.\overline{25}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (61) A deposit of 35 dollars is made at the beginning of each month for 4 years into an account that pays 1.5% interest, compounded 12 times a year. Find the balance in the account at the end of the 4 years.
- (62) The annual net profit for a company from 1998 to 2002 can be approximately by the model, $a_n = 10 e^{0.2n}$, n = 1, 2, 3, ..., N where a_n is the annual net profit in millions of dollars and n represents the year with n = 1 corresponding to 1998. Estimate the total net profit earned during this period.
- (63) A deposit of 15 dollars is made at the beginning of each month for 5 years into an account that pays 0.9% interest, compounded 12 times a year. Find the balance in the account at the end of the 5 years.

 $\underline{\text{Math } 201\text{-}203\text{-}\text{RE}}$

- (64) The annual net profit for a company from 1995 to 2000 can be approximately by the model, $a_n = 5 e^{0.1n}$, n = 1, 2, 3, ..., N where a_n is the annual net profit in millions of dollars and n represents the year with n = 1 corresponding to 1995. Estimate the total net profit earned during this period.
- (65) A deposit of 20 dollars is made quarterly for 10 years into an account that pays 1% interest, compounded 4 times a year.Find the balance in the account at the end of the 10 years.
- (66) A deposit of \$500 can be made with two options: earns 2% interest, compounded monthly for 3 years or earns 1.5% interest, compounded quarterly for 3 years. Find the balance after 3 years of both options.
- (67) A deposit of \$1200 can be made with two options: earns 1.6% interest, compounded bi-monthly for 5 years or earns 2.3% interest, compounded semi-annually for 5 years. Find the balance after 5 years of both options.
- (68) To create a scholarship of \$600 to be awarded every year, use the series $\sum 600 e^{-0.05n}$ to determine the sum of money required to deposit at a rate of 5% interest per year compounded continuously. Find the sum.
- (69) To create a scholarship of \$2000 to be awarded every year, use the series $\sum 2000 e^{-0.03n}$ to determine the sum of money required to deposit at a rate of 3% interest per year compounded continuously. Find the sum.
- (70) A patient is given 5 units of a drug daily for a long period of time. A portion of the drug remains in the patient's body after n years is given by $\sum 5 e^{-n/2}$. Find the total amount of drug remaining in the patient's body after 4 years and also after 15 years.
- (71) A deposit of 10 dollars is made at the beginning of each month for 6 years into an account that pays 1% interest, compounded 12 times a year. Find the balance in the account at the end of the 6 years.
- (72) The annual net profit for a company from 1997 to 2003 can be approximately by the model, $a_n = 15 e^{0.3n}$, n = 1, 2, 3, ..., N where a_n is the annual net profit in millions of dollars and n represents the year with n = 1 corresponding to 1997. Estimate the total net profit earned during this period.
- (73) A deposit of 30 dollars is made at the beginning of each month for 7 years into an account that pays 1.1% interest, compounded 12 times a year. Find the balance in the account at the end of the 7 years.
- (74) The annual net profit for a company from 1996 to 2001 can be approximately by the model, $a_n = 6 e^{0.05n}$, n = 1, 2, 3, ..., N where a_n is the annual net profit in millions of dollars and n represents the year with n = 1 corresponding to 1996. Estimate the total net profit earned during this period.
- (75) A deposit of 50 dollars is made bi-weekly for 8 years into an account that pays 1.3% interest, compounded every two weeks a year.Find the balance in the account at the end of the 8 years.
- (76) A deposit of \$700 can be made with two options: earns 1.8% interest, compounded bi-weekly for 4 years or earns 2.1% interest, compounded monthly for 4 years. Find the balance after 4 years of both options.

 $\underline{\text{Math } 201\text{-}203\text{-}\text{RE}}$

- (77) A deposit of \$1500 can be made with two options: earns 1.4% interest, compounded quarterly for 6 years or earns 1.9% interest, compounded monthly for 6 years. Find the balance after 6 years of both options.
- (78) To create a scholarship of \$750 to be awarded every year, use the series $\sum 750 e^{-0.04n}$ to determine the sum of money required to deposit at a rate of 4% interest per year compounded continuously. Find the sum.
- (79) To create a scholarship of \$1500 to be awarded every year, use the series $\sum 1500 e^{-0.035n}$ to determine the sum of money required to deposit at a rate of 3.5% interest per year compounded continuously. Find the sum.
- (80) A patient is given 4 units of a drug daily for a long period of time. A portion of the drug remains in the patient's body after n years is given by $\sum 4e^{-n/5}$. Find the total amount of drug remaining in the patient's body after 6 years and also after 20 years.

$$\begin{array}{ll} (81) \lim_{x \to 0} \frac{x^2 - e^{2x} + \cos x}{3x^2 + \sin(3x)} \\ (82) \int_0^\infty \frac{4x}{(x^2 + 1)^4} \, dx \\ (83) \int_1^4 \frac{3x}{(1 - x^2)^2} \, dx \\ (84) \int_{-2}^0 \frac{6x}{\sqrt{4 - x^2}} \, dx \\ (85) \lim_{x \to \pi} \frac{\sin x - \tan x}{\cos x - \sin x + 1} \\ (86) \lim_{x \to -1} \frac{x^3 + x^2 + 4x + 4}{x^3 + 3x^2 + 6x + 4} \\ (87) \lim_{x \to -\infty} \frac{4x^2 - e^{3x}}{e^{2x} + 3x^2} \\ (88) \lim_{x \to \infty} \frac{(2x - 1)^3}{(4x + 1)^3} \\ (89) \int_2^{+\infty} \frac{4 \, dx}{x \, (\ln x)^2} \\ (90) \int_0^{\pi/6} \frac{3 \cos x}{(2 \sin x)^{1/3}} \, dx \\ (91) \text{ Determine whether the sequence } a_n = \frac{\sqrt{9n^2 + 2}}{2n + 5} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (92) \text{ Determine whether the sequence } a_n = \frac{4 \, (n - 1)!}{3n!} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (93) \text{ Determine whether the sequence } \left\{\frac{1}{2} \cdot 5^{n+1}\right\}_{n=2}^{+\infty} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (94) \text{ Determine whether the sequence } a_n = 4 \left(\frac{1}{3}\right)^{n-1} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (95) \text{ Determine whether the sequence } \left\{\frac{4n + 5}{2^{n-1}}\right\}_{n=1}^{+\infty} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (95) \text{ Determine whether the sequence } \left\{\frac{4n + 5}{2^{n-1}}\right\}_{n=1}^{+\infty} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (96) \text{ Determine whether the sequence } \left\{\frac{4n + 5}{\sqrt{3} + 4n^2}\right\}_{n=1}^{+\infty} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (96) \text{ Determine whether the sequence a_n = \frac{5 + n}{\sqrt{3} + 4n^2}} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (96) \text{ Determine whether the sequence a_n = \frac{5 + n}{\sqrt{3} + 4n^2}} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (96) \text{ Determine whether the sequence a_n = \frac{5 + n}{\sqrt{3} + 4n^2}} \text{ converges or diverges.} \\ \text{ If the sequence converges, find its limit.} \\ (96) \text{ Determine whether the sequence a_n = \frac{5 + n}{\sqrt{3} + 4n^2}} \text{ converges or diverges.}$$

- (97) Given a repeated decimal $10.2\overline{3}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (98) Given a repeated decimal $7.3\overline{4}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (99) Given a repeated decimal $12.30\overline{2}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.
- (100) Given a repeated decimal $20.0\overline{21}$, express it as a geometric series, find the sum of the geometric series and write the decimal as the ratio of two integers.